No. of Printed Pages: 3

MCS-033

MCA (Revised)

3717

Term-End Examination December, 2010

MCS-033 : ADVANCED DISCRETE MATHEMATICS

Time: 2 hours

Maximum Marks: 50

Note: Question no. 1 is compulsory. Attempt any three questions from the rest.

1. (a) Find the order and degree of the following 6 recurrences. Also, state whether they are homogeneous or non-homogeneous.

(i)
$$a_n = a_{n-1}^2 + a_{n-2} a_{n-3} a_{n-4}$$

(ii)
$$a_{n} = \sqrt{a_{n-1}} + a_{n-2}^2$$

- (b) State and prove the Handshaking theorem. 4
- (c) Define r-regular graph. Give an example 3 of 3-regular graph.
- (d) Solve the recurrence relation $a_{n+1} = 5a_n$ for $n \ge 0$, given that $a_0 = 2$.

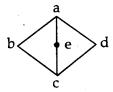
(e) Find the generating function for the sequence given as follows:

2

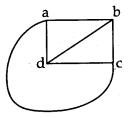
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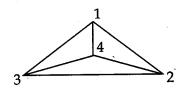
- (f) Define bridge in a graph. Also give an example of it.
- (a) Show that for a Subgraph H of graph G
 Δ(H) ≤Δ(G)
 - (b) Solve the recurrence relation $a_n = a_{n-1} + 2, n \ge 2$ Subject to initial condition $a_1 = 3$.
- 3. (a) Solve the following recurrence relation: $a_n = a_{n-1} + 5^n$, $a_0 = 1$
 - (b) Solve the recurrence relation $a_n = a_{n-1} + n$, $a_0 = 2$ using Substitution method.
- 4. (a) Using generating function solve the 3 following $a_n-4a_{n-1}=0,\ n\geq 1,\ a_0=1$
 - (b) Solve the recurrence $a_{n-9}a_{n-1} + 26a_{n-2} 24a_{n-3} = 0$ for $n \ge 3$

(c) Find Euler Path in the following graph 3 systematically:



- 5. (a) Give an example of graph having Euler's 3 circuit and Hamiltonian Circuit both.
 - (b) Are the following graph are isomorphic? 4
 If yes, Justify your answer.





(c) Construct a graph with chromatic 3 number 5.