

Course Code	:	BCS-042
Course Title	:	Introduction to Algorithm design
Assignment Number	:	BCA(IV)/042/Assignment/2024-25
Maximum Marks	:	100
Weightage	:	30%
Last date of Submission	:	31 st October, 2024 (For July Session)
	:	30 th April, 2025 (For January Session)

This assignment has 8 questions of 10 Marks each, answer all questions. Rest 20 marks are for viva voce. Please go through the guidelines regarding assignments given in the Programme Guide for the format of presentation.

Q1. For the function defined by

$$f(n) = 2n^3 + 3n^2 + 1 \quad \text{and} \quad g(n) = 2n^3 + 1: \quad \text{show that}$$

(i) $f(n) = \Theta(g(n))$

(ii) $f(n) \neq \Theta(n^2)$

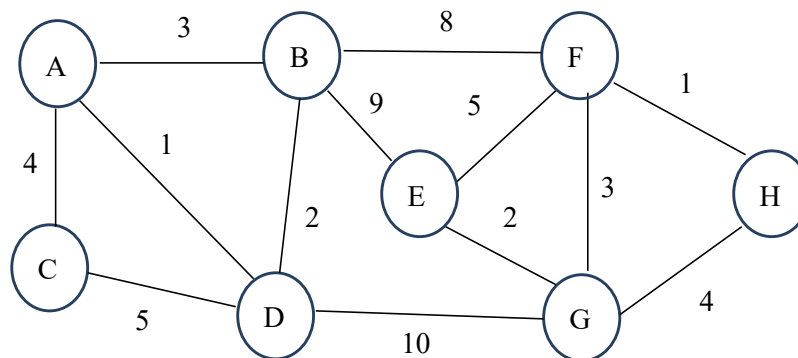
(iii) $n^4 \neq \Theta(g(n))$

Q2. Find the optimal solution for the knapsack instance $n=7$ and $M=15$

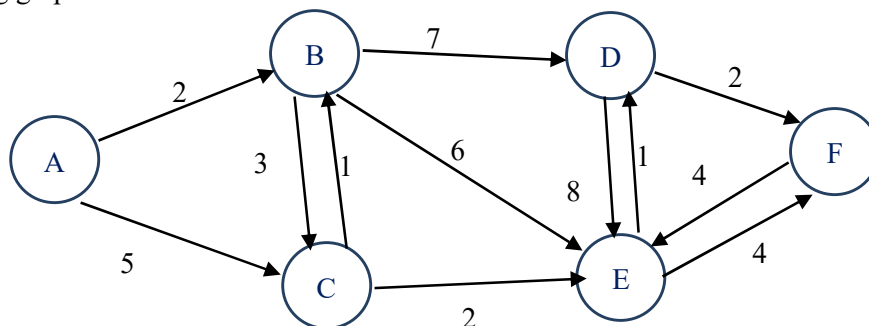
$$(P_1, P_2, \dots, P_n) = (12, 4, 14, 8, 9, 20, 3)$$

$$(W_1, W_2, \dots, W_n) = (3, 2, 5, 6, 4, 1, 7)$$

Q3. Apply Kruskal's Algorithm on the following graph to find minimum cost spanning tree



Q4. Apply Dijkstra's Algorithm to find the shortest path from source vertex 'A' to all other vertices for following graph.



Q5. Analyze best case, average case, and worst-case time complexities of following algorithms with the help of suitable examples.

(i) Insertion sort

- (ii) Quick sort
- (iii) Binary search
- (iv) Selection sort

- Q6.** Multiply 2146782×0422812 using divide and conquer technique (use karatsuba method).
- Q7.** Explain DFS and BFS graph traversal algorithms with the help of a suitable example.
- Q8.** Write recurrence relations for matrix multiplication using Strassen's method and solve it using the Master method.