MASTER IN COMPUTER APPLICATIONS (MCA) (REVISED)

Term-End Examination

December, 2024

MCS-033 : ADVANCED DISCRETE MATHEMATICS

Time: 2 Hours Maximum Marks: 50

Note: Question No. 1 is compulsory. Answer any three questions from the rest.

- 1. (a) Show that $K_{m,n}$ is not Hamiltonian when m+n is odd.
 - (b) Explain the term 'Planar Graphs'. Is a subgraph of a planar graph, planar? Why?

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- (c) Answer the following; with suitable justification:
 - (i) Is a Eulerian graph, Hamiltonian?
 - (ii) Is an Hamiltonian graph, Eulerian?

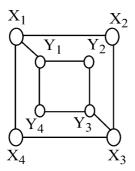
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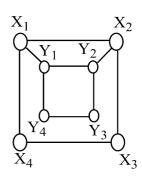
(d) Solve the recurrence relation:

$$F_n = 5F_{n-1} - 6F_{n-2}$$
,

where $F_0 = 1$ and $F_1 = 4$.

- (e) Use power series method to determine the number of integer solutions to the linear equation $X_1+X_2=3$ with $0 \le X_1 \le 1$ and $0 \le X_2 \le 2$.
- (a) Write Handshaking theorem and use it to verify the statement "Any graph can only have an even number of odd vertices."
 - (b) Briefly discuss the travelling salesman problem with suitable example. 5
- 3. (a) Explain the term 'isomorphism'. Are the following graph isomorphic?





- (b) Find cheomatic no. of the following: 5

 (i) a tree with at least two vertices

 (ii) an even cycle C_{2n} , $n \ge 2$ 4. (a) Solve the recurrence relation: 5 $a_n = n^3 a_{n-1}$, $n \ge 1$, $a_0 = 2$ (b) Solve the recurrence relation $T_n = 2T_{n-1} + 1$, if $n \ge 2$ and $T_1 = 1$, using generating
- functions technique. 5
- 5. Write short notes on the following, with suitable example for each: $5\times2=10$
 - (i) Walk
 - (ii) Path
 - (iii) Circuit
 - (iv) Cycles
 - (v) Edge Connectivity